

Titrimetric analysis.

Acid-base titration

Titrimetry

A method based on determination of the volume of reagent reacting stoichiometrically with the analyte

First appeared in XVIII century and did not receive wide acceptance



A –determined compound;

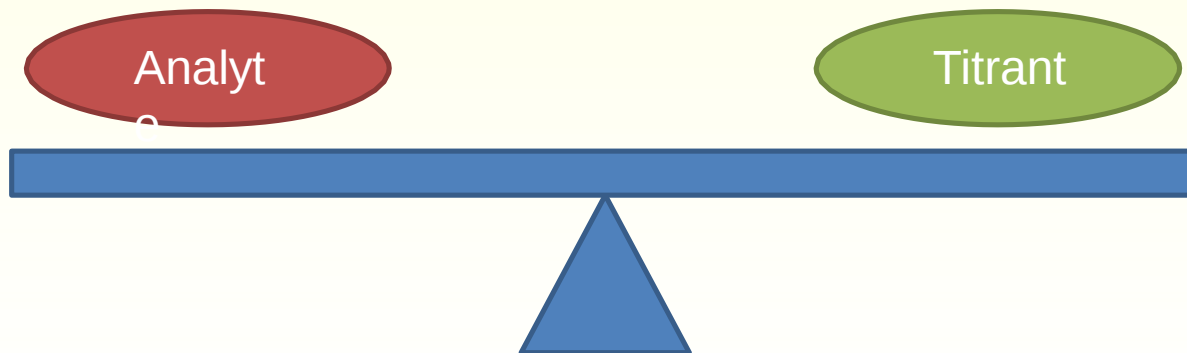
B–added reactant, totally consumed during reaction;

B is added till the moment when it stops reacting with A.

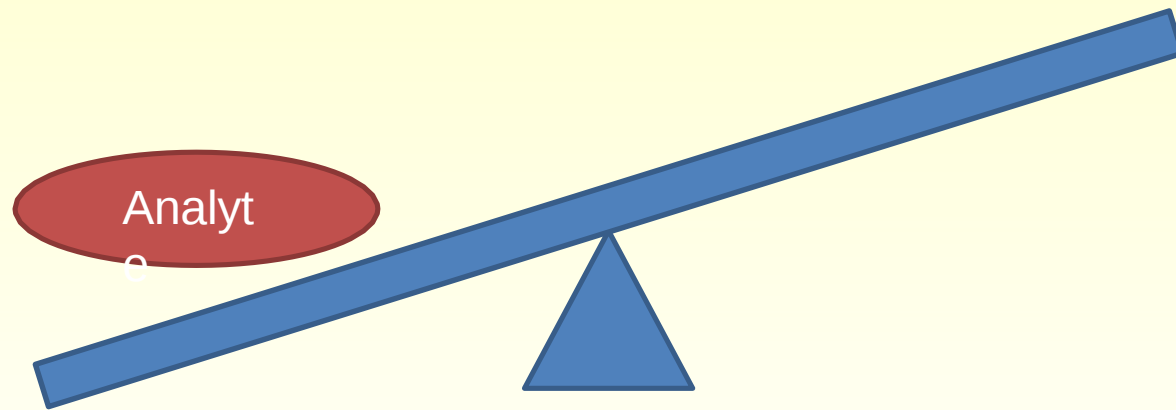
Method principle

Measures volume of a titrant at the equivalence point

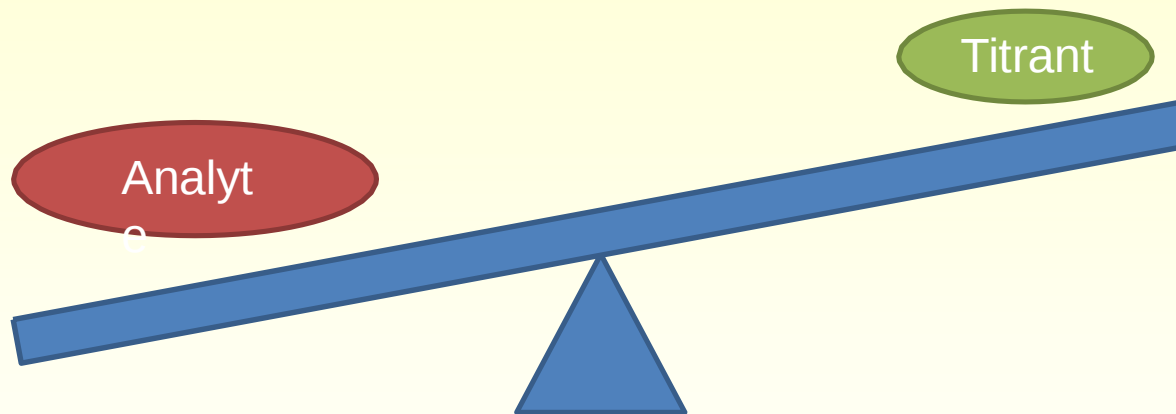
Titrant is added until all analyte is reacted



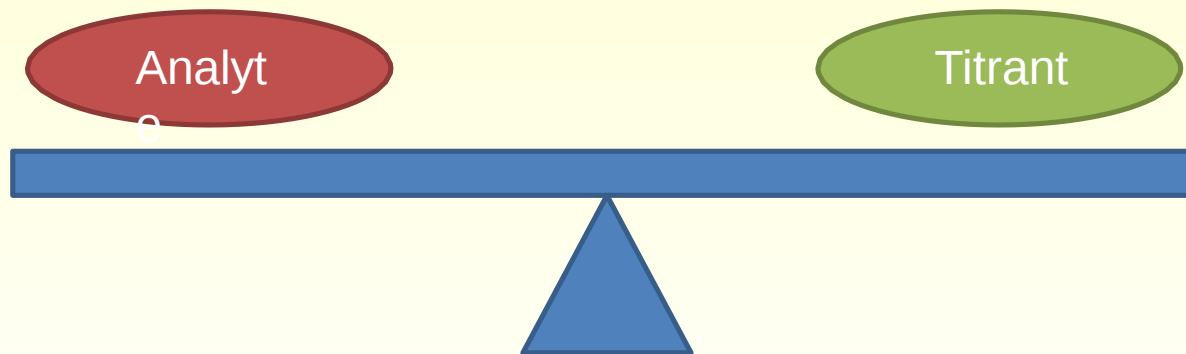
Before titration



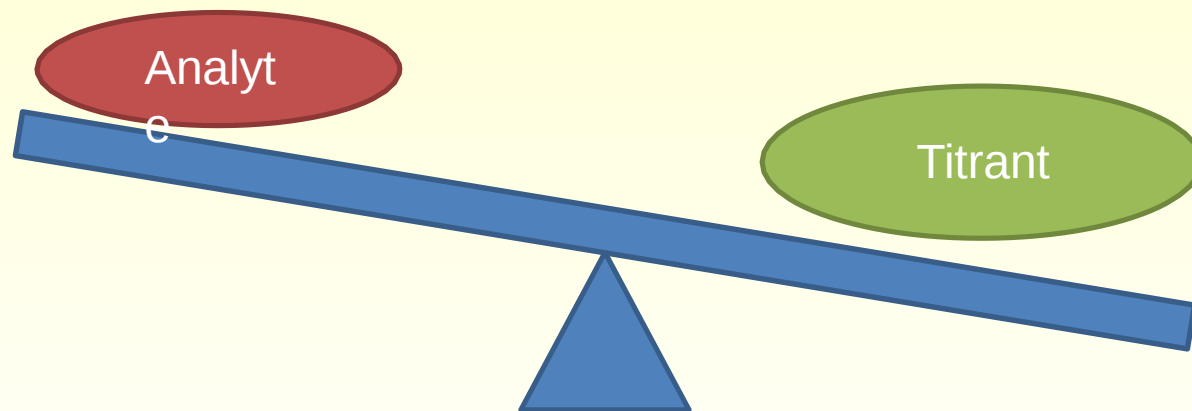
Before equivalence point



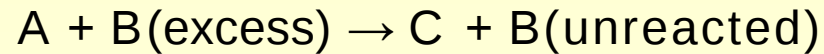
At equivalence point



After equivalence point



Back-titration



After reaction ends, concentration of unreacted “B” is determined by titrimetry (or any other method)

Equivalence point

The most important part of titration – to determine equivalence point

$$\text{Moles of titrant} = V_{\text{eq}} \times C_{\text{T}}$$

where V_{eq} – volume of titrant at equivalence point, L (or mL);

C_{T} – concentration of the titrant, mol/L (or mol/mL)

Equivalence point is determined using:

- indicators (change color at the equivalence point);
- pH measurement;
- electrochemical potential measurement.

Calculation of analyte concentration



$$C_A \times V_A = \frac{C_B \times V_B \times X}{Y}$$

where:

C_A – concentration of analyte in sample (unknown, determined);

V_A – volume of sample (taken by analyst, known);

C_B – concentration of titrant (prepared by analyst, known);

V_B – volume of titrant at the equivalence point (determined);

X and Y – stoichiometric coefficients

Analytical signal

$$S = k \cdot C$$

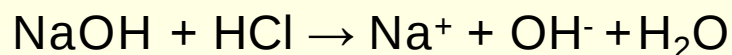
Volume of titrant (V_t) is the analytical signal

$$V_t = \frac{C_A \times V_A \times Y}{C_t \times X}$$

$$k = \frac{V_A \times Y}{C_t \times X}$$

Exercise

10 mL of NaOH solution in water with unknown concentration was titrated with aqueous solution of HCl ($C = 0.200 \text{ mol/L}$). Equivalence point was established at the volume of titrant 7.80 mL. What is the concentration of NaOH in the analyzed sample?



$$C_{\text{NaOH}} = \frac{C_t \times V_t \times X}{V_{\text{NaOH}} \times Y} = \frac{0.200 \frac{\text{mol}}{\text{L}} \times 7.8 \text{ mL}}{10 \text{ mL}} = 0.156 \text{ mol/L}$$

Answer: concentration of NaOH in the analyzed solution is 0.156 mol/L

Quick task

15 mL of H_2SO_4 solution in water with unknown concentration was titrated with aqueous solution of NaOH ($C = 0.200 \text{ mol/L}$). Equivalence point was established at the volume of titrant 12.20 mL. What is the concentration of H_2SO_4 in the analyzed sample?

Titrant volume measurement: burette

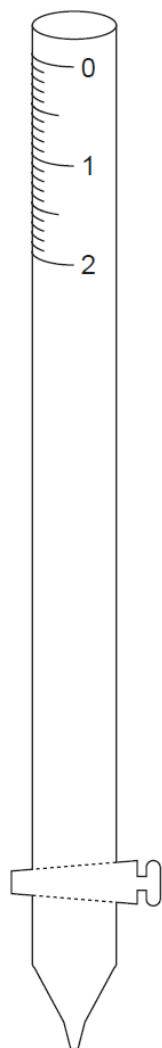
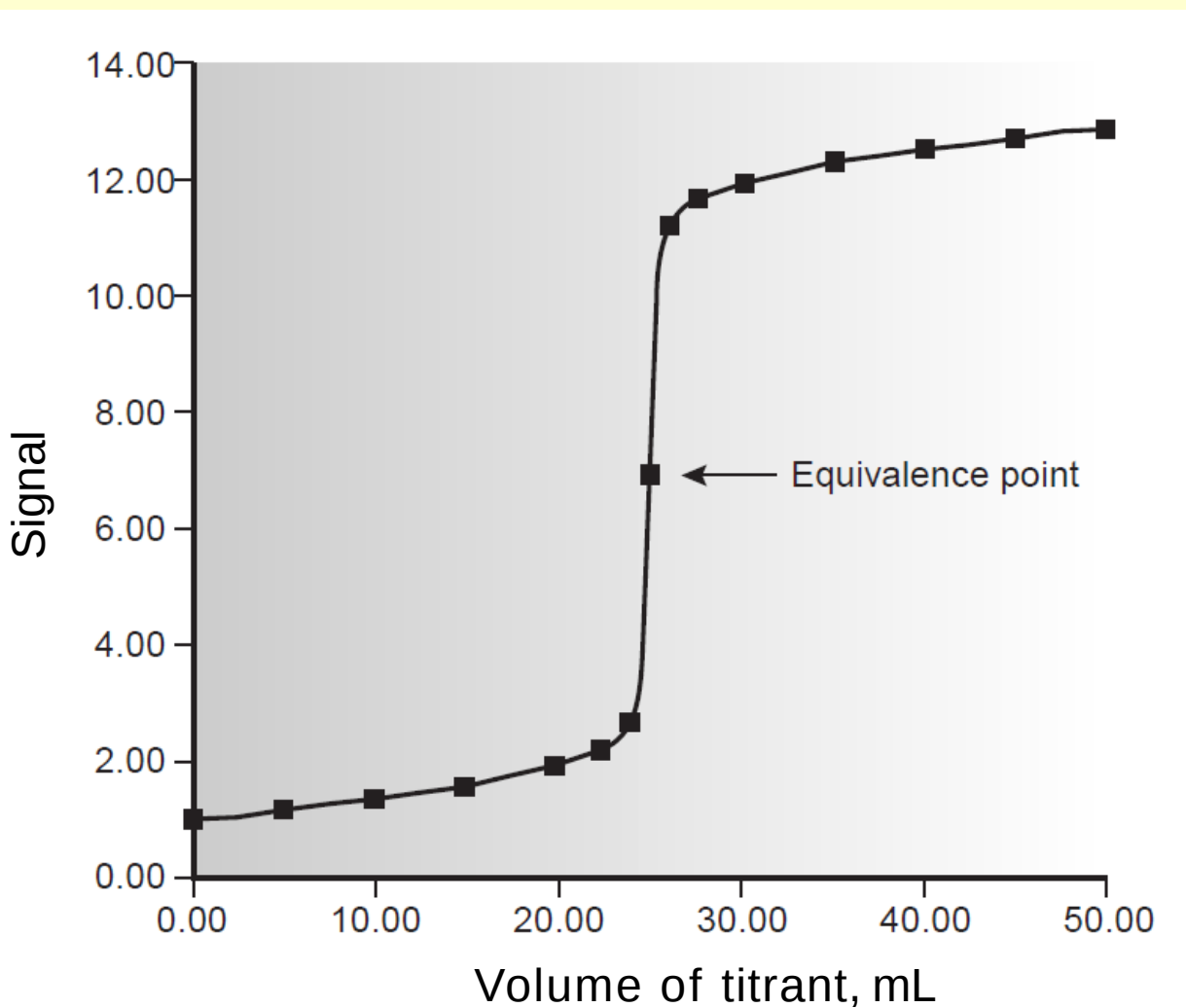


Table 9.1 Specifications for Volumetric Burets

Volume (mL)	Class ^a	Subdivision (mL)	Tolerance (mL)
5	A	0.01	±0.01
	B	0.01	±0.02
10	A	0.02	±0.02
	B	0.02	±0.04
25	A	0.1	±0.03
	B	0.1	±0.06
50	A	0.1	±0.05
	B	0.1	±0.10
100	A	0.2	±0.10
	B	0.2	±0.20

^aSpecifications for class A and class B glassware are taken from American Society for Testing Materials (ASTM) E288, E542, and E694 standards.

Titration curve



Reactions in titrimetry

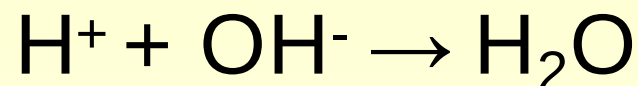
Acid-base

Redox

Complexation

Precipitation

Acids-Base Titrimetry



Acid is titrated by base

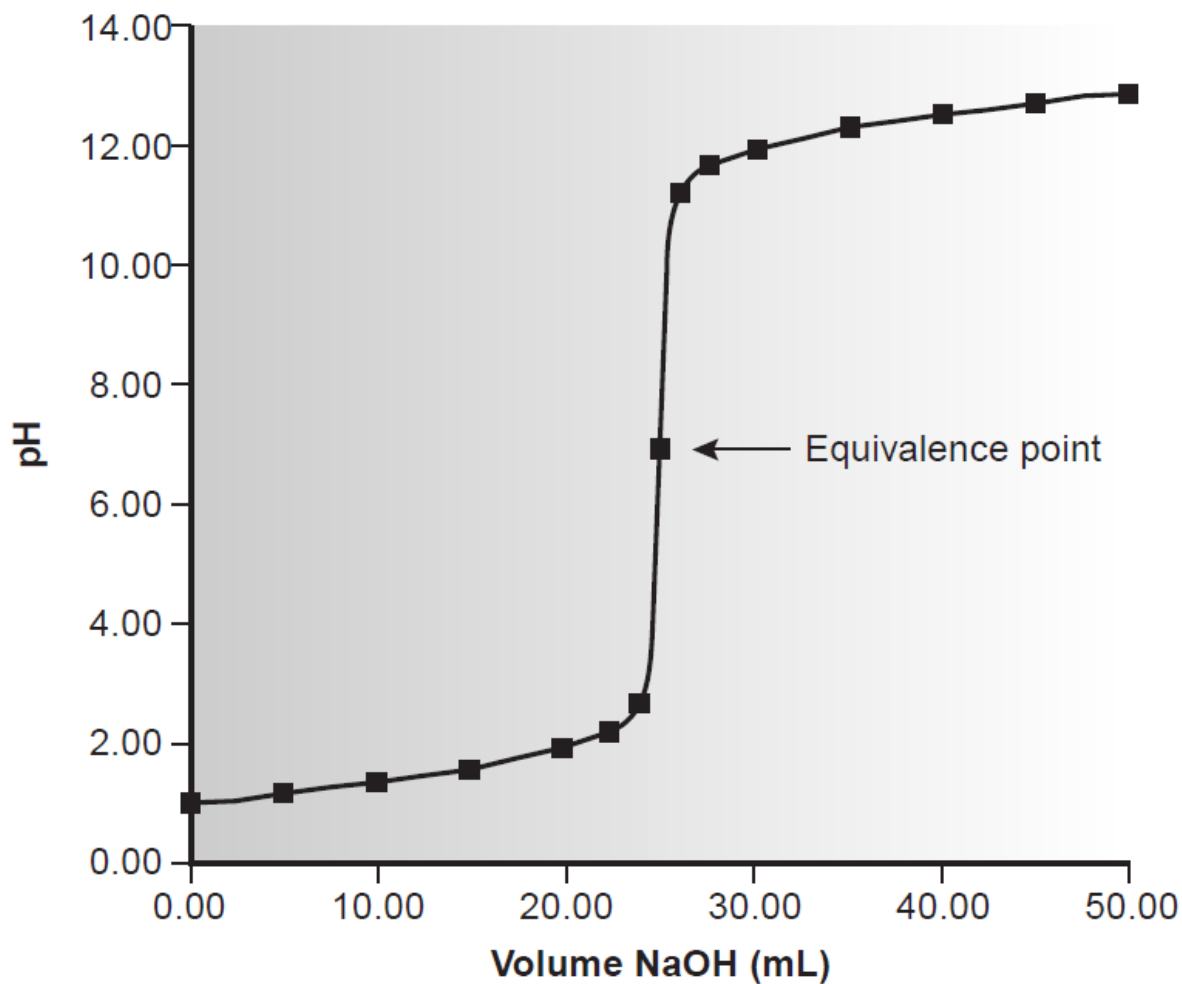
or

Base is titrated by acid

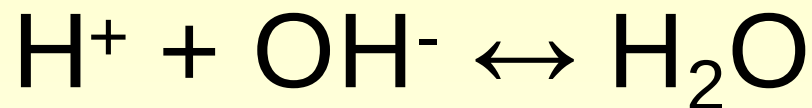
During acid-base titration, pH slowly changes;

At equivalence point pH rapidly changes.

Acid-base titration curve



pH during titration of strong acid



Before equivalence point:

$$\text{pH} = -\log [\text{H}^+] = -\log [\text{unreacted HCl}]$$

After equivalence point:

$$\text{pH} = 14 + \log [\text{OH}^-] = 14 + \log [\text{excess NaOH}]$$

At equivalence point:

$$[\text{H}^+] \times [\text{OH}^-] = 10^{-14}; [\text{H}^+] = [\text{OH}^-] = 10^{-7}$$

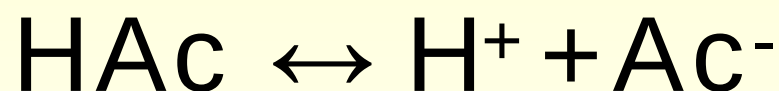
$$\text{pH} = 7$$

Table 9.2**Data for Titration of 50.00 mL of
0.100 M HCl with 0.0500 M NaOH**

Volume (mL) of Titrant	pH
0.00	1.00
5.00	1.14
10.00	1.30
15.00	1.51
20.00	1.85
22.00	2.08
24.00	2.57
25.00	7.00
26.00	11.42
28.00	11.89
30.00	12.50
35.00	12.37
40.00	12.52
45.00	12.62
50.00	12.70

pH during titration of weak acid by strong base

Before titration

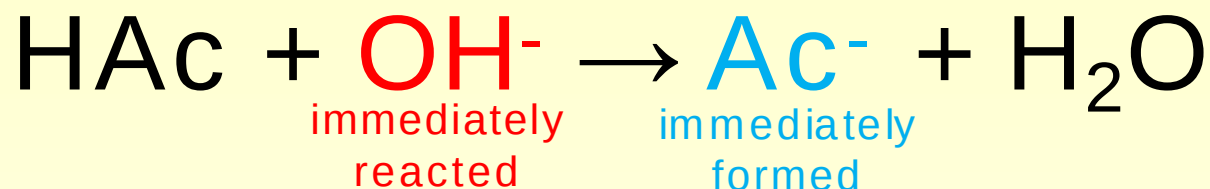


$$K_A = \frac{[\text{H}^+] \times [\text{Ac}^-]}{[\text{HAc}]} = \frac{[\text{H}^+] \times [\text{H}^+]}{C_0 - [\text{H}^+]} = 1.75 \times 10^{-5}$$

For most weak acids $[\text{H}^+] = \sqrt{K_a C_0}$

if $C_0 = 0.1\text{M}$, $[\text{H}^+] = 1.32 \times 10^{-3}$;
 $\text{pH} = -\log [\text{H}^+] = 2.88$

Before an equivalence point



$$K_a = \frac{[\text{H}^+][\text{Ac}^-]}{[\text{HAc}]} \rightarrow [\text{H}^+] = \frac{K_a [\text{HAc}]}{[\text{Ac}^-]}$$

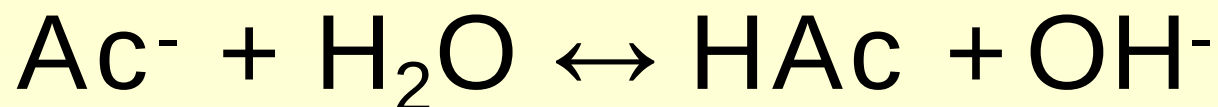
$$\text{pH} = \text{p}K_a + \log \frac{[\text{Ac}^-]}{[\text{HAc}]}$$

$$[\text{HAc}] = \frac{\text{moles of unreacted HAc}}{\text{total volume}} = \frac{C_A \times V_A - C_B \times V_b}{V_A + V_B}$$

$$[\text{Ac}^-] = \frac{\text{moles of NaOH added}}{\text{total volume}} = \frac{C_B \times V_b}{V_A + V_B}$$

$$\text{pH} = \text{p}K_a + \log \frac{\text{moles of NaOH added}}{\text{moles of unreacted HAc}}$$

At and after equivalence point



$$K_b = \frac{[\text{HAc}] \times [\text{OH}^-]}{[\text{Ac}^-]} = \frac{[\text{OH}^-] \times [\text{OH}^-]}{\frac{C_0 \times V_A}{V_A + V_B} - [\text{OH}^-]}$$

$$K_b = \frac{[\text{HAc}] \times [\text{OH}^-]}{[\text{Ac}^-]} = \frac{[\text{HAc}][\text{OH}^-][\text{H}^+]}{[\text{Ac}^-][\text{H}^+]} = \frac{K_w}{K_a} = \frac{10^{-14}}{1.75 \times 10^{-5}} = 5.71 \times 10^{-10}$$

For most weak bases: $[\text{OH}^-] = \sqrt{K_b C_0}$

After an equivalence point, pH will correspond to the concentration of excess NaOH.

$$[\text{OH}^-] = \frac{C_A \times V_A - C_B \times V_B}{V_A + V_B}$$

Table 9.3 Data for Titration of 50.0 mL of 0.100 M Acetic Acid with 0.100 M NaOH

Volume of NaOH (mL)	pH
0.00	2.88
5.00	3.81
10.00	4.16
15.00	4.39
20.00	4.58
25.00	4.76
30.00	4.94
35.00	5.13
40.00	5.36
45.00	5.71
48.00	6.14
50.00	8.73
52.00	11.29
55.00	11.68
60.00	11.96
65.00	12.12
70.00	12.22
75.00	12.30
80.00	12.36
85.00	12.41
90.00	12.46
95.00	12.49
100.00	12.52

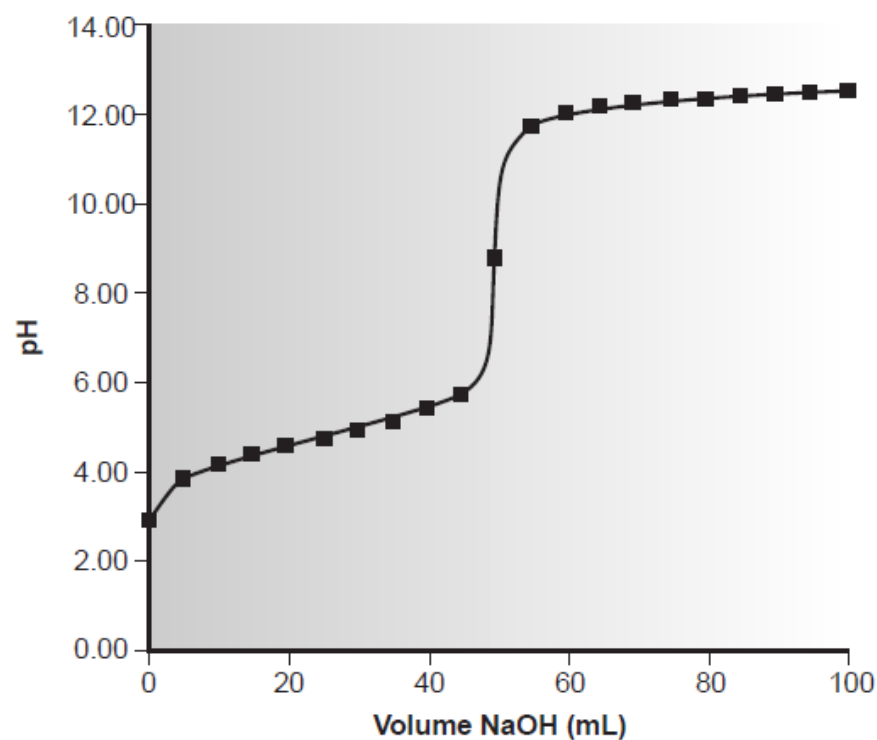
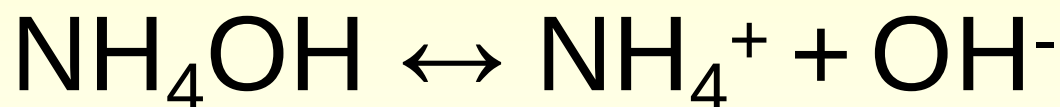


Figure 9.6

Titration curve for 50.0 mL of 0.100 M acetic acid ($pK_a = 4.76$) with 0.100 M NaOH.

pH during titration of weak base by strong acid

Before titration



$$K_b = \frac{[\text{NH}_4^+] \times [\text{OH}^-]}{[\text{NH}_4\text{OH}]} = \frac{[\text{OH}^-] \times [\text{OH}^-]}{C_0 - [\text{OH}^-]} = 1.76 \times 10^{-5}$$

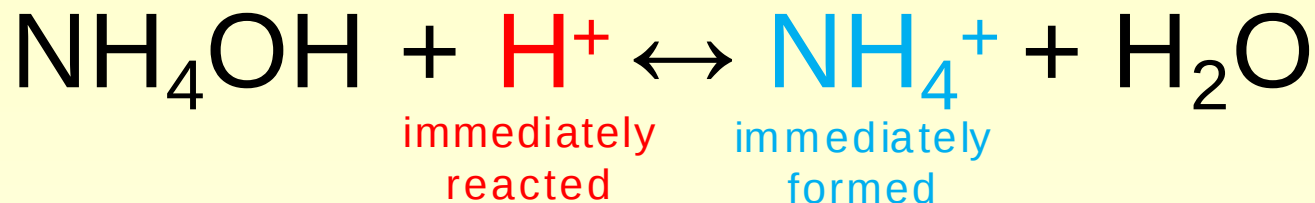
$$\text{For most weak bases: } [\text{OH}^-] = \sqrt{K_b C_0}$$

$$\text{if } C_0 = 0.1\text{M}, [\text{OH}^-] = 1.32 \times 10^{-3};$$

$$\text{pOH} = -\log [\text{OH}^-] = 2.88$$

$$\text{pH} = 14 - \text{pOH} = 11.12$$

Before an equivalence point



$$K_b = \frac{[\text{NH}_4^+][\text{OH}^-]}{[\text{NH}_4\text{OH}]} \rightarrow [\text{OH}^-] = \frac{K_b[\text{NH}_4\text{OH}]}{[\text{NH}_4^+]}$$

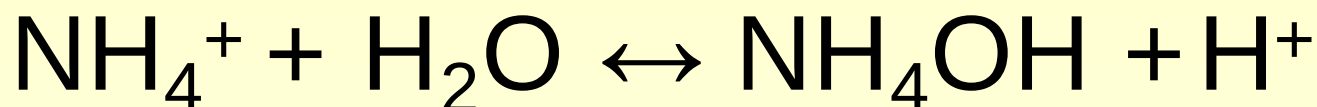
$$\text{pOH} = \text{p}K_b + \log \frac{[\text{NH}_4^+]}{[\text{NH}_4\text{OH}]} \rightarrow \text{pH} = 14 - \text{p}K_b + \log \frac{[\text{NH}_4\text{OH}]}{[\text{NH}_4^+]}$$

$$[\text{NH}_4\text{OH}] = \frac{\text{moles of unreacted NH}_4\text{OH}}{\text{total volume}} = \frac{C_A \times V_A - C_B \times V_B}{V_A + V_B}$$

$$[\text{NH}_4^+] = \frac{\text{moles of HCl added}}{\text{total volume}} = \frac{C_B \times V_B}{V_A + V_B}$$

$$\text{pH} = 14 - \text{p}K_b + \log \frac{\text{moles of unreacted NH}_4\text{OH}}{\text{moles of HCl added}}$$

At and after equivalence point



$$K_a = \frac{[\text{NH}_4\text{OH}] \times [\text{H}^+]}{[\text{NH}_4^+]} = \frac{[\text{H}^+] \times [\text{H}^+]}{\frac{C_0 \times V_A}{V_A + V_B} - [\text{H}^+]}$$

$$K_a = \frac{[\text{NH}_4\text{OH}][\text{H}^+]}{[\text{NH}_4^+]} = \frac{[\text{NH}_4\text{OH}][\text{H}^+][\text{OH}^-]}{[\text{NH}_4^+][\text{OH}^-]} = \frac{K_w}{K_b} = \frac{10^{-14}}{1.76 \times 10^{-5}} = 5.68 \times 10^{-10}$$

For most weak acids: $[\text{H}^+] = \sqrt{K_a C_0}$

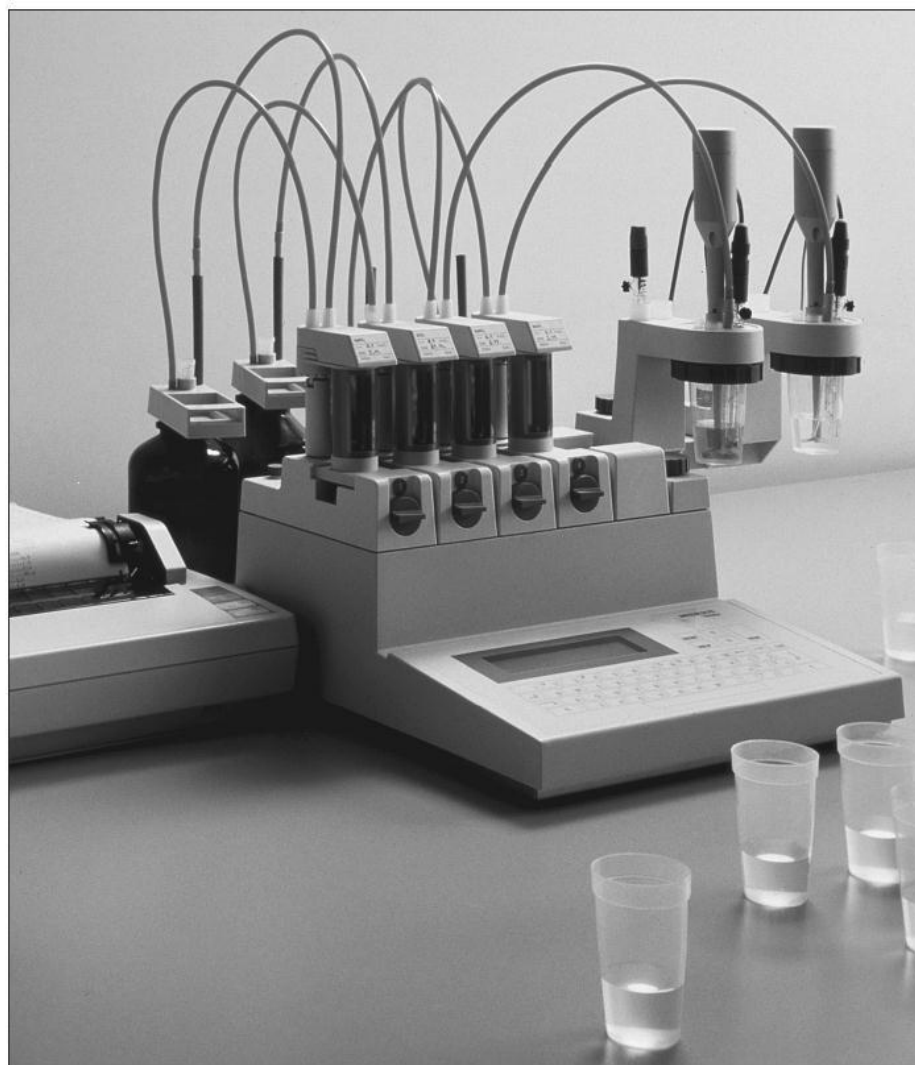
After equivalence point, pH will correspond to the concentration of excess HCl.

$$[\text{H}^+] = \frac{C_A \times V_A - C_B \times V_B}{V_A + V_B}$$

Table 9.4 Properties of Selected Indicators, Mixed Indicators, and Screened Indicators for Acid–Base Titrations

Indicator	Acid Color	Base Color	pH Range	pK _a
cresol red	red	yellow	0.2–1.8	—
thymol blue	red	yellow	1.2–2.8	1.7
bromophenol blue	yellow	blue	3.0–4.6	4.1
methyl orange	red	orange	3.1–4.4	3.7
Congo red	blue	red	3.0–5.0	—
bromocresol green	yellow	blue	3.8–5.4	4.7
methyl red	red	yellow	4.2–6.3	5.0
bromocresol purple	yellow	purple	5.2–6.8	6.1
litmus	red	blue	5.0–8.0	—
bromothymol blue	yellow	blue	6.0–7.6	7.1
phenol red	yellow	red	6.8–8.4	7.8
cresol red	yellow	red	7.2–8.8	8.2
thymol blue	yellow	blue	8.0–9.6	8.9
phenolphthalein	colorless	red	8.3–10.0	9.6
alizarin yellow R	yellow	orange/red	10.1–12.0	—
Mixed Indicator		Acid Color	Base Color	pH Range
bromocresol green and methyl orange		orange	blue-green	3.5–4.3
bromocresol green and chlorophenol red		yellow-green	blue-violet	5.4–6.2
bromothymol blue and phenol red		yellow	violet	7.2–7.6
Screened Indicator		Acid Color	Base Color	pH Range
dimethyl yellow and methylene blue		blue-violet	green	3.2–3.4
methyl red and methylene blue		red-violet	green	5.2–5.6
neutral red and methylene blue		violet-blue	green	6.8–7.3

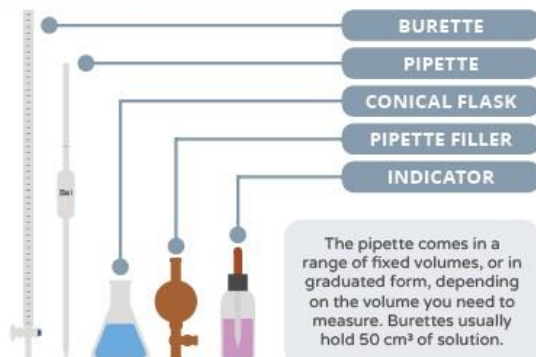
Autotitrator



CHEMISTRY TECHNIQUES: TITRATION

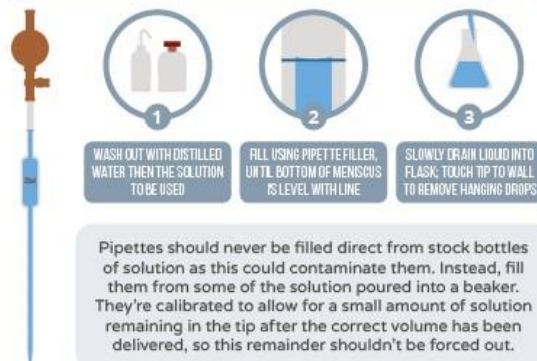
Used to determine the concentration of a particular solution, by measuring how much of a solution of known concentration reacts with a known volume of it.

EQUIPMENT



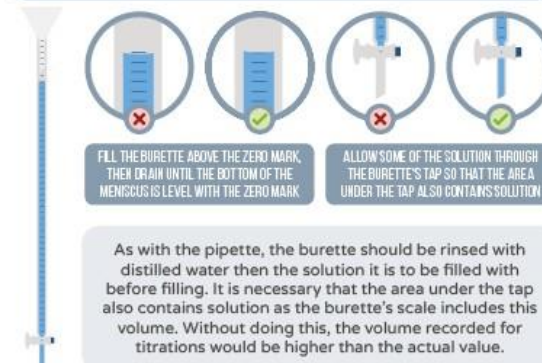
The pipette comes in a range of fixed volumes, or in graduated form, depending on the volume you need to measure. Burettes usually hold 50 cm³ of solution.

USING A PIPETTE



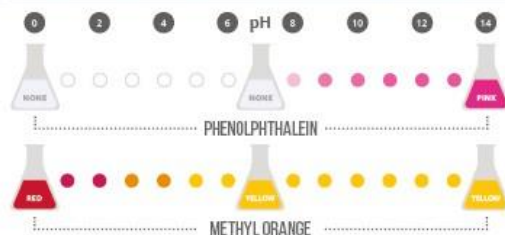
Pipettes should never be filled direct from stock bottles of solution as this could contaminate them. Instead, fill them from some of the solution poured into a beaker. They're calibrated to allow for a small amount of solution remaining in the tip after the correct volume has been delivered, so this remainder shouldn't be forced out.

FILLING THE BURETTE



As with the pipette, the burette should be rinsed with distilled water then the solution it is to be filled with before filling. It is necessary that the area under the tap also contains solution as the burette's scale includes this volume. Without doing this, the volume recorded for titrations would be higher than the actual value.

USING INDICATORS



In acid-base titrations, a range of indicators can be used. These are solutions which change colour at a specific pH, and can be used to precisely identify when the neutralisation reaction is complete (the end point). Different indicators are suitable for different acid-base combinations.

CARRYING OUT THE TITRATION



To carry out the titration, the tap of the burette is opened to allow the solution inside to flow into a known volume of the solution in the conical flask. The amount of solution from the burette required to reach the end point is recorded. A rough titration is usually followed by more accurate runs. Multiple titrations are carried out until concordant titres are obtained (within 0.10 cm³ of each other).

CARRYING OUT CALCULATIONS

